

Discussion: Compare Two CFGs



Expression	→ IntegerConstant BooleanConstant BinaryOp UnaryOp (Expression)
IntegerConstant	→ Digit Digit IntegerConstant -IntegerConstant
Digit	→ 0 1 2 3 4 5 6 7 8 9
BooleanConstant	→ TRUE FALSE

BinaryOp	→ Expression + Expression Expression - Expression Expression * Expression Expression / Expression Expression && Expression Expression Expression Expression ==> Expression Expression == Expression Expression /= Expression Expression > Expression Expression < Expression
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UnaryOp	→ ! Expression
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v2

ArithmeticOp	→ ArithmeticOp + ArithmeticOp ArithmeticOp - ArithmeticOp ArithmeticOp * ArithmeticOp ArithmeticOp / ArithmeticOp (ArithmeticOp) IntegerConstant
RelationalOp	→ ArithmeticOp == ArithmeticOp ArithmeticOp /= ArithmeticOp ArithmeticOp > ArithmeticOp ArithmeticOp < ArithmeticOp
LogicalOp	→ LogicalOp && LogicalOp LogicalOp LogicalOp LogicalOp ==> LogicalOp ! LogicalOp (LogicalOp) RelationalOp BooleanConstant

Context-Free Grammar (CFG): Example Version 1

Example: $(1 + 2) \Rightarrow (5 / 4)$

Expression → *IntegerConstant*
 | *BooleanConstant*
 | *BinaryOp*
 | *UnaryOp*
 | (*Expression*)

IntegerConstant → *Digit*
 | *Digit IntegerConstant*
 | -*IntegerConstant*

Digit → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

BooleanConstant → TRUE
 | FALSE

BinaryOp → *Expression* + *Expression*
 | *Expression* - *Expression*
 | *Expression* * *Expression*
 | *Expression* / *Expression*
 | *Expression* && *Expression*
 | *Expression* || *Expression*
 | *Expression* => *Expression*
 | *Expression* == *Expression*
 | *Expression* /= *Expression*
 | *Expression* > *Expression*
 | *Expression* < *Expression*

UnaryOp → ! *Expression*

Context-Free Grammar (CFG): Example Version 1

Example: $3 * 5 + 4$

Expression → *IntegerConstant*
 | *BooleanConstant*
 | *BinaryOp*
 | *UnaryOp*
 | (*Expression*)

IntegerConstant → *Digit*
 | *Digit IntegerConstant*
 | -*IntegerConstant*

Digit → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

BooleanConstant → TRUE
 | FALSE

BinaryOp → *Expression* + *Expression*
 | *Expression* - *Expression*
 | *Expression* * *Expression*
 | *Expression* / *Expression*
 | *Expression* & & *Expression*
 | *Expression* | | *Expression*
 | *Expression* => *Expression*
 | *Expression* == *Expression*
 | *Expression* /= *Expression*
 | *Expression* > *Expression*
 | *Expression* < *Expression*

UnaryOp → ! *Expression*

Context-Free Grammar (CFG): Example Version 2

Example: $(1 + 2) \Rightarrow (5 / 4)$

<i>Expression</i>	→	<i>ArithmeticOp</i>
		<i>RelationalOp</i>
		<i>LogicalOp</i>
		<i>(Expression)</i>
<i>IntegerConstant</i>	→	<i>Digit</i>
		<i>Digit IntegerConstant</i>
		<i>-IntegerConstant</i>
<i>Digit</i>	→	0 1 2 3 4 5 6 7 8 9
<i>BooleanConstant</i>	→	TRUE
		FALSE

<i>ArithmeticOp</i>	→	<i>ArithmeticOp</i> + <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> - <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> * <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> / <i>ArithmeticOp</i>
		<i>(ArithmeticOp)</i>
		<i>IntegerConstant</i>
<i>RelationalOp</i>	→	<i>ArithmeticOp</i> == <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> /= <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> > <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> < <i>ArithmeticOp</i>
<i>LogicalOp</i>	→	<i>LogicalOp</i> && <i>LogicalOp</i>
		<i>LogicalOp</i> <i>LogicalOp</i>
		<i>LogicalOp</i> => <i>LogicalOp</i>
		! <i>LogicalOp</i>
		<i>(LogicalOp)</i>
		<i>RelationalOp</i>
		<i>BooleanConstant</i>

Context-Free Grammar (CFG): Example **Version 2**

Expression → *ArithmeticOp*
 | *RelationalOp*
 | *LogicalOp*
 | (*Expression*)

IntegerConstant → *Digit*
 | *Digit IntegerConstant*
 | *-IntegerConstant*

Digit → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

BooleanConstant → TRUE
 | FALSE

ArithmeticOp → *ArithmeticOp* + *ArithmeticOp*
 | *ArithmeticOp* - *ArithmeticOp*
 | *ArithmeticOp* * *ArithmeticOp*
 | *ArithmeticOp* / *ArithmeticOp*
 | (*ArithmeticOp*)
 | *IntegerConstant*
RelationalOp → *ArithmeticOp* == *ArithmeticOp*
 | *ArithmeticOp* /= *ArithmeticOp*
 | *ArithmeticOp* > *ArithmeticOp*
 | *ArithmeticOp* < *ArithmeticOp*
LogicalOp → *LogicalOp* && *LogicalOp*
 | *LogicalOp* || *LogicalOp*
 | *LogicalOp* => *LogicalOp*
 | ! *LogicalOp*
 | (*LogicalOp*)
 | *RelationalOp*
 | *BooleanConstant*

Q: No semantic analysis at all
for Version 2 grammar?

Context-Free Grammar (CFG): Example Version 2

Example: $3 * 5 + 4$

<i>Expression</i>	→	<i>ArithmeticOp</i>
		<i>RelationalOp</i>
		<i>LogicalOp</i>
		(<i>Expression</i>)
<i>IntegerConstant</i>	→	<i>Digit</i>
		<i>Digit IntegerConstant</i>
		- <i>IntegerConstant</i>
<i>Digit</i>	→	0 1 2 3 4 5 6 7 8 9
<i>BooleanConstant</i>	→	TRUE
		FALSE

<i>ArithmeticOp</i>	→	<i>ArithmeticOp</i> + <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> - <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> * <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> / <i>ArithmeticOp</i>
		(<i>ArithmeticOp</i>)
		<i>IntegerConstant</i>
<i>RelationalOp</i>	→	<i>ArithmeticOp</i> == <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> /= <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> > <i>ArithmeticOp</i>
		<i>ArithmeticOp</i> < <i>ArithmeticOp</i>
<i>LogicalOp</i>	→	<i>LogicalOp</i> && <i>LogicalOp</i>
		<i>LogicalOp</i> <i>LogicalOp</i>
		<i>LogicalOp</i> => <i>LogicalOp</i>
		! <i>LogicalOp</i>
		(<i>LogicalOp</i>)
		<i>RelationalOp</i>
		<i>BooleanConstant</i>

Context-Free Grammar (CFG): Example Version 3

$Expr$	$\rightarrow$	$Expr + Term$
	$ $	$Term$
$Term$	$\rightarrow$	$Term * Factor$
	$ $	$Factor$
$Factor$	$\rightarrow$	$(Expr)$
	$ $	a

Example: $a * a + a$

Context-Free Grammar (CFG): from RE (1)

RE	CFG
$L(\epsilon)$	
$L(a)$	
$L(E + F)$	
$L(EF)$	
$L(E^*)$	
$L((E))$	

Context-Free Grammar (CFG): from RE (2)

$(0 + 1)^* 1(0+1)$

$(00 + 1)^* + (11 + 0)^*$

Context-Free Grammar (CFG): from DFA

